



Running away from the rest when it rained is how The Professor won the Pilote Elf

*A Hypothesis and candidate for*

# A Theory of Slow Turns in Automobile Road Racing

<http://theoryofracing.com>

*"It is amazing how many drivers, even at the Formula One level, think that the brakes are for slowing the car down."* -- Mario Andretti

## Abstract

This paper presents the claim that there is an application of Game Theory to the problem of negotiating turns which follow maximum braking, known as slow turns, in the fastest possible way.

## Limitations

The Theory of Slow Turns applies only to cars whose designs subscribe to the Theory of Slow Turns. In other words:

- In theory, the Theory of Slow Turns applies only to cars which are points or bricks or otherwise enjoy a perfect distribution of mass which places their CG at their centroid, or directly below it.
- In practice, the Theory of Slow Turns applies only to mid-engine cars with front wheel steering.

## Disclaimer

Do not try this in your Porsche.

# Prerequisite Information

There are two pieces of background knowledge the reader must have at this point: the definition of slow turns, and the braking and turning force fundamentals.

## 1. Definitions

**Fast turn:** A turn for which you as the driver would not lift. A clean example of a fast turn can be seen at 1:27 [here](#)

**Medium turn:** One for which you would lift and perhaps brake lightly to moderately

**Slow turn:** One for which you would brake hard and deep into; perhaps  $\frac{1}{3}$  -  $\frac{1}{2}$  way. A clean example of a slow turn can be seen at 0:24 [here](#)

## 2. Force Vectors

This theory accepts as correct the assertions regarding the forces acting upon the car made in "The Technique of Motor Racing" by Piero Taruffi[1].

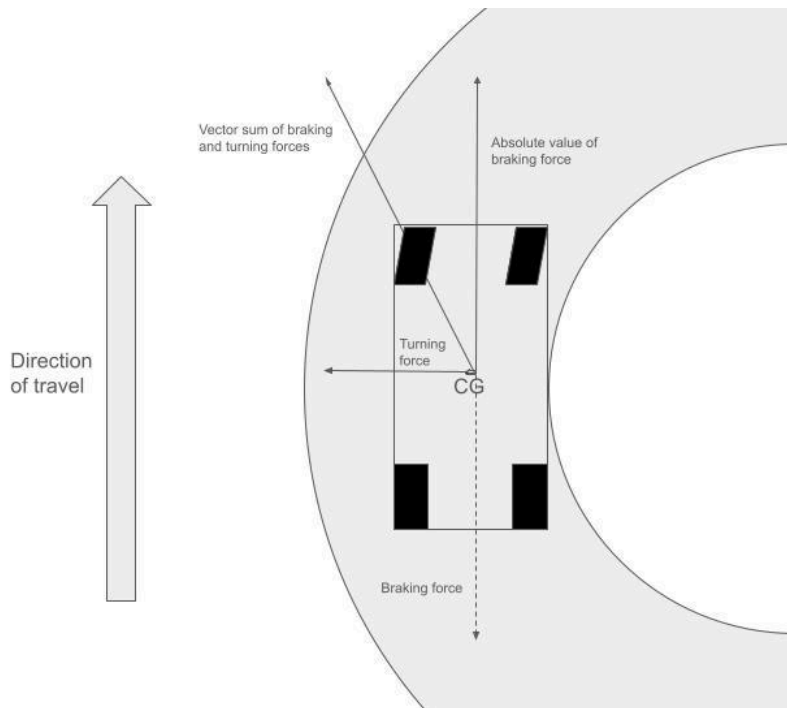


Figure 1. Forces acting on a car in a turn.

**Figure 1** shows the forces. The braking force is towards the rear of the car; we are more interested in its absolute value. Taruffi claims that when the magnitude of the vector sum of the braking and turning force vectors exceeds the available traction, the car will lose adhesion and leave the road in the direction of the vector sum. This diagram presently has this error: the car is shown in the middle of the turn, when the brakes should be fully off, but the braking force vector is not drawn with zero length.

# Theory

## *1(a) Postulate 1*

At the end of the straightaway the driver must be braking as hard as is possible without locking the wheels. In other words using, by braking, as much of the available traction as is possible without using it all.

## *1(b) Postulate 2*

At the apex of the turn the car should be going around the turn as fast as possible without losing adhesion and leaving the road. In other words using - by turning - as much of the available traction as is possible without using it all.

## *1(c) Assertion*

The optimal driver behavior between the entrance of the turn and the apex is to release the brakes in such a way that the magnitude of the vector sum of the braking and turning forces is kept constantly requiring as close as is possible to but without equalling 100% of the available traction.

## *1(d) Corollary Hypothesis*

For any given car, for every recognizable slow turn we can identify, there is an {optimal de-braking curve, fastest entry speed} pair.

# Comments

“Thus, for Poker players, Game Theory bears fruit. Game Theory tells us that for every recognizable poker situation we can name, there is an optimal strategy. The strategy may be too complex for us to discern, but in theory there is one.”

- Ankeny, Nesmith: *Poker Strategy: Winning with Game Theory*

Game Theory also tells us that for every slow turn that we can identify, there exists an optimal de-braking strategy.

This theory claims that that strategy is to let no amount of available traction go unused. If traction goes unused then either the driver failed to either brake or turn as hard as was possible, or the entry speed was too low.

Further, if we subscribe to *The Theory of Inceasable Traction*, then: where it was the former - the brakes could have been used harder - there was also less resultant downforce from the braking that didn't happen - so less traction, compounding the penalty for this sin.

We have, then, that regarding Corollary 1(d), the single fastest de-braking curve simultaneously permits and requires the single fastest entry speed.

It is not a game of pushing down. It is a game of lifting up. I suppose this should have been obvious a priori, given the normal state of the pedal in a race is on the floor.

*Release the brakes as you would approach God.*

## Exercises

1. Watch the slow turn example of Fernando Alonso many times as is necessary - slowing the playback speed and pausing as necessary - to see that he spends the entire second from 0:27 to 0:28 simultaneously releasing the brakes and turning the wheel in. One can hear the RPMs continue to drop after he downshifts into 1st, between 0:26.0 and 0:26.5, until the apex right at 0:27.9.  
[▶ fernando alonso onboard pole lap at magny cours 2005](#)
2. Sit in a chair with no arms and scoot forward so your sitbones are near the front edge of the seat. Hold your right foot on an already depressed imaginary brake pedal, with your heel 1" above the floor. Hold your hands at the 3 and 9 o'clock positions on an imaginary steering wheel.
3. When you are ready, suddenly but smoothly begin to lift your foot up a few inches and turn the wheel 90 degrees at the same time. Do it at a rate that both finish in exactly one full second.  
When lifting your foot, do not use your foot or ankle - use the muscles in your thigh or hip, letting everything from your kneecap down hang.  
Lifting your foot and turning the wheel at the same time is like rubbing your stomach and patting your head at the same time. It is not difficult but nobody gets it right the first time. If you wish to use it to your advantage you must practice it ahead of time..
4. Now try making it take two seconds, and try one-half of a second.
5. Now do it over 1 second but starting slowly and ending quickly, then do it starting quickly and ending slowly.
6. Do them again but turn the wheel 180 degrees.
7. Before you get good at it, come to San Jose, CA, and race me at indoor go-karts. We'll do 20 laps for \$100/lap, switching cars after 10. Bring \$2K to lose to me and rest assured it will be worth every penny.
8. Now watch this video of Lewis Hamilton in turn 11 at Suzuka at 0:13 here  
[▶ Lewis Hamilton Smashes Suzuka Track Record | 2017 Japanese Grand Prix](#)  
Whether that is a video game or too much camera firmware is making it look like one; either way, what is going on with that de-braking curve?
9. Now go back to Alonso and watch his steering between 0:26.5 and 0:27. He turns the wheel 90 degrees first, before 0:27, then 90-100 more after, but is the rate constant? It first looks to me like there is a pause, but if I focus on his hands not the steering wheel center, they appear to move at a constant rate.
10. Now forward to 0:57 as he approaches the Chateau d'Oh. A few moments later the announcer will say he has never seen a car turn in so well. How might it be possible to reword "so well"?

## Known Bugs

This theory contains at least one error, but this may be it.

## Note

This paper is about racing, and specifically not about driving on the street. It is, for the most part, not useful on the street; for example, the style of driving required to apply it includes entering a turn much faster than the average speed through the corner, and exiting significantly slower. But other traffic expects you to keep a more or less consistent speed.

Furthermore at street speeds it is difficult to compress springs enough to have an unloading time long enough for you to work with. For example, suppose you are cruising down main street, Anytown, and approaching a 4-way intersection where the speed limit is 30 in all directions. For your cruising speed to be 105-115 would be neither safe nor legal nor practical. Were you to then brake quite hard down to 60 at the white line, compressing the front springs by a goodly amount, and then meter out that stored energy in the downward direction by modulating the brakes and exiting the turn at a crawl - 10 or 15 - because 60 was too slow, and you refused to let the front bob up (and failed to let it creep back up without bobbing in the time you had left when you realized) - or something like that - if this describes your street driving then, well, there is simply no way around it. You belong in prison.

## Authenticity

If you have any questions or concerns regarding the authenticity of the information presented here, I suggest you direct your inquiries to Elf/Renault Winfield Ecole du Pilotage, or to Mika Hakkinen, Fernando Alonso, Alain Prost, Nelson Piquet, Gerhard Berger, Nigel Mansell, Riccardo Patrese, Eddie Cheever, Rene Arnoux, or Jean Alesi, or the McLaren, Williams, Ferrari, Brabham, Lotus, or Lola Racing teams.

## References

1. [The Technique of Motor Racing](#), Taruffi, Piero, 1959
2. [Poker Strategy: Winning with Game Theory](#), Nesmith Ankeny, 1982
3. <http://theoryofracing.com/images/elfrenault.png>, ELF-Renault, 1989
4. [The ELF/Renault Winfield Ecole du Pilotage](#), 1964-
5. [Expert C programming -Deep C secrets](#), Peter van der Linden, 1994